

Pairings

1. Which of the following properties does a pairing $e: G_1 \times G_2 \rightarrow G_T$ have? (Mark as many options as you think are correct.)

- (A) Bilinearity
- (B) Collision-resistance
- (C) Non-degeneracy

2. How many evaluations of a pairing $e: G \times G \rightarrow G_T$ does each party have to perform in Joux's 3-party key exchange protocol to compute a shared key?

3. (Requires knowledge about common cryptographic assumptions in cyclic groups.) Intuitively, a pairing allows one "multiplication in the exponent", at the cost of moving to another group G_T . Why is a pairing with $G_1=G_2=G_T$ (and $e(g,g)=g$) probably not very useful?

In the lecture, we asked this question without the $e(g,g) = g$ requirement. The answer for the case $e(g,g) \neq g$ stays the same, but requires a more complex argument (see solution file).